

Diastereodivergent Construction of Bicyclic γ -Lactones via Enantioselective Ketone Hydroacylation

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Supporting Information

ABSTRACT: We present a diastereodivergent strategy for constructing bicyclic γ -lactones bearing quaternary carbon centers via ketone hydroacylation. By applying a Rh catalyst and JoSPOphos ligand, either the *anti* or *syn* bicyclic γ -lactones can be accessed with high enantio- and diastereoselectivities, depending on the choice of solvent, temperature, and counterion.

C yclic architectures comprise a large number of natural products with diverse biological activity.¹ Nature uses enzymes to access both stereoisomers of any bicycle through kinetic control.² The use of metal catalysis to construct bicyclic motifs with high enantio- and diastereocontrol thus represents a modern challenge for organic synthesis. Inspired by the occurrence of bicyclic γ -lactones in natural products³ (Figure 1a), we sought an atom-economical strategy⁴ to access both the



Figure 1. Inspiration for diastereodivergent formation of bicyclic γ -lactones.

syn and anti diastereomers by ketone hydroacylation⁵⁻⁷ (Figure 1b). Toward this goal, we herein report the construction of bicyclic γ -lactones featuring the rare activation of aliphatic aldehydes, without competitive decarbonylation.^{7,8}

To begin our studies, we chose 4,4'-diketo aldehyde **1a** bearing a β -quaternary carbon center as the model substrate. This substrate would allow us to address the challenge of preparing quaternary carbon centers with high enantiocontrol using desymmetrization.^{9–11} Guided by previous hydroacylations,^{6,7} we examined [Rh(C₂H₄)₂Cl]₂ with a wide range of bidentate phosphine ligands.¹² The Josiphos family of ligands, which we previously found to promote *intermolecular* hydroacylation with aliphatic aldehydes, proved promising (Table 1).¹² A combina-

Table 1. Ligand Effects on Stereoselectivity^{*a,b*}



^{*a*}Isolated yields. The *ee* was determined by chiral SFC analysis, and *dr* was determined by ¹H NMR analysis of the unpurified reaction mixture. ^{*b*}Conditions: **1a** (0.20 mmol), $[Rh(C_2H_4)_2Cl]_2$ (2.5 mol %), ligand (5 mol %) in toluene (0.4 mL), 21 °C, 24 h.

tion of $[Rh(C_2H_4)_2Cl]_2$ and Josiphos L1 in toluene afforded the *anti* bicyclic γ -lactone **2a** (25% yield, >20:1 *dr*, 56% *ee*). Using Josiphos L2 improved the enantioselectivity (32% yield, >20:1 *dr*, 87% *ee*). With JoSPOphos L3,¹³ both diastereomers were observed with excellent enantioselectivities (98% *ee* for **2a** and 99% *ee* for **3a**) in 89% yield as a 3:1 mixture of **2a:3a**. Developed by Pugin and Pfaltz for asymmetric hydrogenation, this ligand had yet to be explored for hydroacylation.¹³

While methods for making bicyclic γ -lactones have been reported,^{14,15} we aimed to develop a complementary and diastereodivergent strategy. Because the JoSPOphos L3 ligand provided access to both anti and syn diastereomers with high enantiocontrol, we chose this ligand for further study. Through a solvent study at 21 °C (Table 2a), we found that the anti diastereomer was favored in polar aprotic solvents, such as 1,2dimethoxyethane (DME) (8:1 2a:3a). In contrast, the syn diastereomer was preferred in polar protic solvents, such as tertamyl alcohol (t-AmOH) (1:3 2a:3a). By applying these solvents, we discovered a strong temperature dependence (Table 2b). At lower temperatures, the anti diastereomer was favored (e.g., 13:1 2a:3a at 10 °C in DME), whereas higher temperatures favored the syn diastereomer (e.g., 1:10 2a:3a at 80 °C in t-AmOH). Finally, tuning of the catalyst counterion revealed that those more coordinating (*e.g.*, Cl⁻) promote **2a**, whereas those less coordinating (*e.g.*, SbF₆⁻) favor **3a** (Table 2c).^{16,17} Ultimately, this intramolecular hydroacylation generates the anti diaster-

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 Table 2. Parameters Impacting Diastereocontrol^{a,b}

a. solvent effect: ([Rh(C ₂ H ₄) ₂ Cl] ₂ , at 21 °C)						
		protic				
2a DME tol	luene DC	E THF		t-BuOH	<i>t</i> -AmOH	3a
anti 8:1	3:1 1.7	:1 1.3:1		1:2	1:3	syn
b. temperature effect: ([Rh(C ₂ H ₄) ₂ Cl] ₂)						
i	in <i>t</i> -AmOH					
⊿ 10 °C	21 °C	80 °C	21 °C	50 °C	80 °C	~
2a <>						> 3a
anti 13:1	8:1	1.5:1	1:3	1:8	1:10	syn
c. counterion effect: (Rh(COD) ₂ X or [Rh(COD)X] ₂)						
in DN	ir	in <i>t</i> -AmOH, at 80 °C				
⊿ CI⁻ I	Br⁻l⁻	SbF ₆ ⁻	Cl⁻	TfO ⁻ E	BF4 ⁻ SbF6 ⁻	N
2a < > 3						
<u>anti</u> 13:1 6	6:1 3:1	2:1	1:11	1:>20 1:	>20 1:>20	syn

^{*a*}Conditions: 1a (0.20 mmol), [Rh] (5 mol %), JoSPOphos L3 (5 mol %) in solvent, 24 h. The diastereomeric ratio (*dr*, 2a:3a) for each case was determined by ¹H NMR analysis of the unpurified reaction mixture. ^{*b*}For isolated yields and *ee*'s of the products, see Table S2 in SI.

eomer **2a** (91% yield, 17:1 *dr*, 99% *ee*) under $[Rh(NBD)Cl]_2/L3$ in DME at 10 °C and the *syn* diastereomer **3a** (98% yield, >20:1 *dr*, 97% *ee*) under Rh(COD)_2SbF₆/L3 in *t*-AmOH at 80 °C.

Next, we examined the scope and prepared 19 *anti* bicyclic γ -lactones in high yields and enantioselectivities (Table 3). Keto

 Table 3. Enantioselective and anti-Diastereoselective Ketone

 Hydroacylation^a



^{*a*}Isolated yields of the major diastereomer **2**. The *ee* was determined by chiral SFC analysis, and *dr* was determined by ¹H NMR analysis of the unpurified reaction mixture. ^{*b*}Conditions: **1** (0.10 or 0.20 mmol), [Rh(NBD)Cl]₂ (2.5 mol %), JoSPOphos **L3** (5 mol %) in DME (0.50 M), 10 °C, 24 h. ^{*c*}Conditions: **1** (0.10 mmol), [Rh(COD)Cl]₂ (2.5 mol %), Josiphos **L1** (5 mol %) in *n*-BuOAc (0.50 M), 100 °C, 24 h.

aldehydes bearing various alkyl groups cyclized to the corresponding *anti* bicyclic γ -lactones in 53–91% yields with 6–17:1 *dr* and 94–>99% *ee* (2a–f). Dimethyl substituted bicyclic γ -lactone 2g was obtained in 81% yield, 6:1 *dr*, >99% *ee*, and its absolute configuration was determined by X-ray crystallography.¹² A keto aldehyde containing a seven-membered

ring underwent the intramolecular hydroacylation to afford bicyclic [5.3.0] lactone **2h** in 59% yield and 98% *ee* but with lower diastereoselectivity (2:1 *anti:syn*). Under the standard conditions, we found that the 3-phenyl substituted keto aldehyde gave the corresponding *syn* bicyclic γ -lactone **3m** rather than the expected *anti* diastereomer **2i**. By using Josiphos **L1** as the ligand in *n*-BuOAc at 100 °C, however, the *anti* diastereomer **2i** was obtained in 81% yield, 10:1 *dr*, and 96% *ee*. Using Josiphos **L1**, substrates with either electron-donating (**2j**, **2k**, **2q**, **2r**) or electron-withdrawing groups (**2l**-**p**) on the phenyl ring gave the desired bicyclic γ -lactones in 67–78% yields with 6–12:1 *dr* and 87–97% *ee*. Aryl halides (**2b**, **2l**, **2m**), ketones (**2e**), esters (**2f**, **2n**), and nitriles (**2o**) were tolerated.

In a similar fashion, we examined the substrate scope under the *syn* diastereoselective conditions (Table 4). Twenty-three 4,4'-





^{*a*}Isolated yields of the major diastereomer **3**. The *ee* was determined by chiral SFC analysis, and *dr* was determined by ¹H NMR analysis of the unpurified reaction mixture. ^{*b*}Conditions: **1** (0.10 or 0.20 mmol), Rh(COD)₂SbF₆ (5 mol %), JoSPOphos **L3** (5 mol %) in *t*-AmOH (0.20 M), 80 °C, 6 h. ^{*c*}[Rh(COD)Cl]₂ (2.5 mol %) was used.

diketo aldehydes gave the desired *syn* bicyclic γ -lactones (**3a**–**w**) in 51–99% yields with >20:1 *dr* and 83–>99% *ee*. Substrates with five- or seven-membered rings efficiently afforded the corresponding *syn* [3.3.0] and [5.3.0] bicyclic γ -lactones (**3k**, 93% yield, >20:1 *dr*, 95% *ee*; **3l**, 95% yield, >20:1 *dr*, >99% *ee*), respectively.¹⁸ Our hydroacylation conditions tolerated ketone (**3g**), ester (**3h–i**, **3q**), halogen (**3b**, **3o**, **3p**, **3t**), nitrile (**3r**), nitro (**3s**), and naphthyl groups (**3c**, **3w**). Some of the aldehydes

showcased here (1e, 1f, 1i, and 1k) were unreactive when tested under the *anti* selective conditions. The *syn* selective protocol shows greater scope most likely due to the higher reaction

under the *anti* selective conditions. The *syn* selective protocol shows greater scope most likely due to the higher reaction temperature. The absolute configuration of **3j** was confirmed by X-ray crystallography.¹² In comparison to the *anti* selective hydroacylation, the enantiotopic carbonyl group undergoes reduction to generate the corresponding *syn* diastereomer (see X-ray data for compound **2g** vs **3j**).¹²

To explore the elaboration of these bicycles, we applied this method to achieve an enantioselective formal synthesis of (-)-mesembrine (Figure 2), which is a potent serotonin



Figure 2. Formal enantioselective synthesis of (-)-mesembrine.

reuptake inhibitor isolated from *Sceletium tortuosum*.^{19,20} We chose to intercept a racemic intermediate from Kulkarni's route.²¹ Rh-catalyzed desymmetrization of the 4,4'-diketo aldehyde **1x** provided *syn* bicyclic γ -lactone **3x** in 92% yield, >20:1 *dr*, 97% *ee*. The absolute configuration of **3x** was confirmed by X-ray crystallography.¹² Pd-catalyzed aerobic dehydrogenation²² and subsequent Luche reduction afforded the allylic alcohol **4**. Sequential, 1,3-transposition of **4** with Osborn's rhenium(VII) catalyst,²³ oxidation, and catalytic hydrogenation afforded isomeric *syn* bicyclic γ -lactone **5**, which has been converted to (–)-mesembrine.²¹

To gain insight into the mechanism, we prepared isotopically labeled substrates and performed crossover and KIE experiments. A crossover experiment with **1b** and **D-1a** suggests that Rh–H insertion is intramolecular, rather than intermolecular.¹² We measured kinetic isotope effects by using a mixture of **1a** and **D-1a**; we observed no KIE under *anti* conditions and a KIE near unity under the *syn* conditions (Figure 3). These results suggest that neither aldehyde C–H bond activation nor Rh-hydride insertion are turnover-limiting.²⁴

On the basis of our observations and previous reports,^{6,7,25} we propose a mechanism in which reductive elimination governs the diastereoselectivity (Figure 4).²⁶ First, oxidative addition of the aldehydic C-H bond in diketo aldehyde 1 to the Rh(I)-catalyst generates an acyl-Rh(III)-hydride intermediate I. Subsequent insertion of the ketone carbonyl group into the Rh-H bond of I generates either rhodacycle II or III. Because the insertion step is reversible, intermediates II and III are in equilibrium. The turnover-limiting and stereodetermining step is reductive elimination, which delivers the bicyclic γ -lactone (2 or 3) and regenerates the Rh(I)-catalyst. Thus, Curtin-Hammett type kinetics may be operative.²⁶ Based on our X-ray crystallography results, enantiotopic carbonyl groups are selected by the same catalyst, which suggests remarkably different transition states leading to the syn versus anti isomers. The solvent and coordinating ability of the counterion influences these transition state geometries and energies. Notably, we also observe a strong



Figure 3. H/D crossover and kinetic isotope effect experiments.



Figure 4. Reductive elimination governs diastereoselectivity.

temperature dependence on diastereoselectivity,²⁷ which may be due to a marked difference in the entropy of activation for these competing reductive eliminations.

By computational studies,²⁸ we find that the *syn* bicycle **3a** is thermodynamically more stable than the *anti* isomer **2a**. We recognize that the *syn* isomer can undergo a chair flip and thus has more conformational degrees of freedom than its *anti* counterpart. A survey of literature reveals that bond formation to generate related fused bicycles typically occurs to the carbonyl via the *same* side of the reactive tether, suggesting that such additions are rapid and irreversible.^{9b} In contrast, our hydroacylation strategy enables access to both stereoisomers via kinetic control. Under our standard conditions, the *anti* and *syn* products do not interconvert,¹² further supporting the idea that reductive elimination is irreversible. Further kinetic and computational studies are underway to better understand these effects to guide development of future stereodivergent strategies.

ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/jacs.6b06227.

Detailed experimental procedures and compound characterization (PDF) Crystallographic data (CIF, CIF, CIF)

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Notes

The authors declare no competing financial interest.

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